

# Strains Induced in Urban Structures by Ultra-high Frequency Blasting Rock Motions; a Case Study

C. H. Dowding

*Professor, Northwestern University, Department of Civil and Environmental Engineering, Evanston, IL, 60208, USA*

E. Hamdi

*Associate Professor, Université de Tunis El Manar – Ecole Nationale d'Ingénieurs de Tunis. LR14ES03-Ingénierie Géotechnique. BP 37 Le Belvédère, 1002 Tunis, Tunisia.*

C. T. Aimone-Martin

*Aimone-Martin Assoc. Socorro, NM, USA*

## ABSTRACT:

This paper describes measurement and interpretation of strains induced in two, multiple story, older, urban structures by ultra-high frequency rock blast excitation from contiguous excavation. These strains are obtained from relative displacements found by integrating time correlated velocity time histories from multiple positions on the structures and foundation rock. Observations are based on ten instrumented positions on the structures and in the foundation rock during eight blast events, which provided over seventy time histories for analysis. The case study and measurements allowed the following conclusions: Despite particle velocities in the rock that greatly exceed regulatory limits, strains in external walls are similar to or lower than those necessary to crack masonry structures and weak wall covering materials. These strains are also lower than those sustained by single story residential structures when excited by low frequency motions with particle velocities below regulatory limits. Expected relative displacements calculated with pseudo velocity single degree of freedom response spectra of excitation motions measured in the rock are similar to those measured.

KEY WORDS: displacements, shear and tensile strains, close-in rock blasting, urban structures, ultra-high frequency excitation, pseudo velocity spectral analysis, peak particle velocity.

## 1 1 INTRODUCTION

2 The case study summarized by this paper provides the multiple position, time-correlated, ve-  
3 locity time histories needed to advance understanding of response of urban structures to ultra-  
4 high frequency excitation. Current regulations and understanding are based upon measure-  
5 ments of the response of residential, 1 to 2 story structures (Siskind, et al 1980, Dowding,  
6 2000). Extension of these observations by response spectrum analysis to taller structures when  
7 excited by high frequency excitation needs to be validated (Abeel, 2012). This paper provides  
8 the beginning of such validation.

9  
10 Most often standard earthquake engineering assumes that excitation wave lengths are long  
11 enough that buildings are excited homogenously and respond synchronously. In other words  
12 excitation motions along the base of the structure are the same and response at the top occurs  
13 synchronously. For close-in rock blasting this is not the case. With high excitation frequencies  
14 ( $> 100$  Hz for rock to rock transmission) the amplitudes and phase are likely to change along  
15 the bottom of the structure. For instance, with a propagation velocity of 3000 m/s, 150 Hz  
16 frequency and a distance along the bottom of the structure of 60 m, the excitation pulse would  
17 have traveled  $(60/(3000/150)=) 3$  wave lengths and might have attenuated significantly (Woods  
18 & Jadele, 1985). In addition the time of arrival would not be equal at the ends of the building  
19 if the blast were detonated at one end. The peak would arrive some  $60/3000 = 20$  milliseconds  
20 later the other end. If the building were 5 stories high and had a fundamental response period  
21 of 0.5 sec., its response at the other end would be  $(0.020/0.5)2\pi$  or  $0.080\pi$  out of phase from  
22 the end where the blast was initiated.

23  
24 This study provides the additional multiple position, time-correlated information to more fully  
25 define the response of these larger, more massive urban structures. Current regulations often  
26 only require that the excitation motions be measured at one location. Building response is then  
27 most likely to be considered as synchronous and similar to that measured by the Siskind's et  
28 al. (1980) work with smaller, less massive structures. There is no requirement to measure build-  
29 ing response, and as a result compliance measurements provide no new information about the  
30 nature of response of larger buildings to ultra-high frequency excitation.

31

1 Discussion of the use of strain-based methods of vibration control can provide regulatory guid-  
2 ance. Changes in regulations based upon strain measurements can reduce the confusion in spec-  
3 ifications, help define the most appropriate locations of measurement of response, and provide  
4 more appropriate construction controls. These changes should help reduce costs of urban con-  
5 struction in rock founded cities around the world.

6  
7 The paper is divided into two main sections: Site& Instrumentation and Response. Site and  
8 Instrumentation is divided into four sections: site and geology, transducers, blasting practice  
9 and vibratory environment. Response is divided into three sections: differential displacement,  
10 strains, comparison with controls.

## 11 2 SITE AND GEOLOGY PRESENTATION

12 This study was conducted in a dense urban location where blasting was required not just adja-  
13 cent to buildings but contiguous to them as shown by the photograph in Figure 1. Blast exca-  
14 vation was carried out at the two sites simultaneously which led to instrumentation of the two  
15 buildings and allowed response from a blast at one site to be measured at both buildings as well  
16 as two locations on the same building. Contiguous blasting produced excitation ground motions  
17 that were unusually high in amplitude and with ultra-high dominant frequencies.

18  
19 The buildings were constructed in 1890 and 1920, and are typical of structures built in this  
20 city at that time. They are 4- to 6-stories high, with load bearing walls constructed of unrein-  
21 forced brick masonry, which are thought to be 2 to 3 wythe thick. Floors of these buildings  
22 were constructed with wood joists. Recently the ground floor of building 2 was reconstructed  
23 as reinforced concrete to support the weight of fire trucks. Both structures have basements,  
24 exterior walls of which are shown by the photographs of the excavations shown in Figure 2

25  
26 The rock supporting these structures is a mica schist whose foliation dips into the excavation  
27 from beneath the structures. It is a dark-gray to silvery, rusty-weathering, generally coarse  
28 grained, foliated but poorly layered to massive gneiss or schistose gneiss, composed of quartz,  
29 oligoclase, microcline, biotite, and muscovite, and generally sillimanite and garnet (Panish,  
30 1992). Vertical rock faces are supported by rock bolts that are 3m to 10m long.

### 3 TRANSDUCER DESCRIPTION AND INSTALLATION

Buildings and rock were instrumented with geophone transducers that meet International Society of Explosive Engineers (ISEE) standards. They measure velocity and have flat responses between 2 and 250 Hz. These transducers were monitored with digital seismographs with output digitized at 2048 samples per second (sps). Seismographs begin recording (6 seconds duration with 0.25 seconds of pre-trigger) when the particle velocity exceeds a threshold. The threshold had to be set variably because of the background noise produced by mechanical, rock excavation through back-hoe ramming. Seismographs were connected in series to provide a common time base that was accurate within one sample interval of 0.0005 sec. When the closest seismograph detects ground motion that exceeds the threshold value, it begins recording and triggers the other sensors.

#### 3.1 *Building 1 transducers*

Two geophones were placed at each of the north and south corners of the west wall nearest the excavation as shown in Figure 2 (a-left). Two were bolted at the building street level (denoted in the following as B (bottom) sensors) and two to the top of the wall (denoted hereafter sensors A). Vertical distance between the sensors B and A differs at the south and north locations because of the differing building geometry. The lower (B) transducers are bolted on brackets which in turn are bolted into the mortar between bricks on the building about 1 m (3-4ft) above street level. The upper (A) transducers are also bolted to brackets and bolted into the mortar onto the inside of the parapet wall just above roof mastic.

Each geophone contained two transducers; one in the radial direction, parallel to the west wall and the other in the transverse direction, perpendicular to the west wall. All four transducers (two upper and two lower) at a corner were connected to one, four channel seismograph to provide a common time stamp. South and north seismographs were connected to provide a common time stamp.

In addition one triaxial geophone was installed in the rock beneath the north corner with the radial parallel and the transverse perpendicular to the west wall. These rock geophones were connected to the building seismographs to provide a common time stamp. Typical construc-

1 tion interference and back-hoe ramming reduced the number of blast events wherein rock meas-  
2 urements were possible during blast events. Also construction interaction prevented installation  
3 of rock transducers altogether at the south end

### 4 3.2 *Building 2 transducers*

5 Building 2 was instrumented in a manner similar to that of building 1 as shown in Figure 2 (b-  
6 right). As with building 1, geophones were placed at the lower (B) and upper (A) parts of the  
7 west wall with radial parallel and transverse perpendicular to the wall. North A transducers  
8 with bolted to the inside of the upper tower portion instead of the parapet location. As with  
9 Building 1, all four transducers (two upper and two lower) at a corner were connected to one,  
10 four channel seismograph to provide a common time stamp. South and north seismographs  
11 were connected to provide a common time stamp.

12  
13 Two other transducers were also bolted to building 2. One transversely sensitive transducer  
14 was bolted to the inside of the basement wall at mid height, 10 m (33 ft) north of the south  
15 wall. A second, vertically sensitive transducer was mounted to the underside to the basement  
16 ceiling (first floor) also 10 m north of the south wall. They were also wired to

17  
18 Additionally, one triaxial geophone was bolted to the vertical rock face beneath building 2 at  
19 the south end and time correlated with structure measurements. This geophone was also ori-  
20 ented with radial parallel and transverse perpendicular to the west wall. As shown in Figure 2,  
21 it was installed 0.9m below the basement floor level.

22  
23 Time correlation connections and timing of transducer installation were difficult to coordinate  
24 with construction and blasting. As is true for instrumentation of any construction project, many  
25 opportunities are lost because of either timing or construction difficulties. There was no pro-  
26 vision for time correlation between the two buildings, as the distance was too large and the  
27 cable route too complex. While much of the data obtained for bottom (B) and top (A) responses  
28 is time correlated, correlation between corners was difficult to obtain because of connection  
29 challenges. Because of late installation, rock response is missing for all but five of the blasts.  
30 Events reported herein are those where all motions of a building were time correlated.

#### 1 4 BLASTING PRACTICE

2 Rock fragmentation and excavation was accomplished with close-in blasting techniques. Blasts  
3 are initiated by a Nonel initiation system. Holes are delayed with 25 and 17 ms surface delays  
4 with 500 ms in-hole delays. A blast typically contains 20-50 holes with 2 to 10 rows. The holes  
5 are arranged in a spacing and burden pattern of less than 60cm x 60cm (2ft x 2ft). There is  
6 usually at least one free vertical face, and often two. Blast holes are charged with a combination  
7 of two explosives types of emulsion explosive. Because of limitations of blast-induced vibra-  
8 tion peak particle velocity, the number of holes per volume of fragmented rock is often high,  
9 hole diameter is small and in-hole delays are used. There were at total of 8 blasts designated a  
10 through h used in this study. Charge weights per delay varied from 2.41 to 2.96 kg. Scaled  
11 distances and absolute distances from the north corner of Building 1 varied from 7.5 to 14.1  
12 ( $\text{m}/\text{kg}^2$ ) and 1.9 to 19.8 for events f and a respectively.

#### 13 5 GROUND MOTION ENVIRONMENT

14 Ground motions monitored in this study produced peak particle velocities (PPV's) that attenu-  
15 ate at expected rates when plotted against square root scaled distance. Ground motion data from  
16 the rock below the structures were available for five of the blasts, four under building 1 and  
17 one under building 2. Figure 3 plots the values of peak velocity against scaled distance for these  
18 five blasts as well as expected values given by Oriard (1972). The lines on the plot are lower  
19 and upper bounds of expected values as well as upper bound of expected values for highly  
20 confined blasts. Four of the five plotted points from this study fall within the normal bounds  
21 of expected values, and all five fall below the upper bound for confined blasts. As these blasts  
22 are indeed confined, these data are in the expected range given by Oriard and are not unusual.

23  
24 These rock to rock motions occur at unusually high frequencies (140 to 500 Hz) and produce  
25 unusually low building response as shown by the response spectra of the rock motions in Figure  
26 4. Rock motions are rarely measured in urban blasting because the geometry of most immedi-  
27 ately adjacent urban excavations only allows measurement at the street (B) level, because rock  
28 is inaccessible at the beginning and changes elevation with the adjacent excavation.

29  
30 There are many possible explanations for the lower PPV's on the building at the street level.  
31 Large mismatches between response and excitation frequencies (0.5 and 500 Hz) results in very  
32 low velocity response as shown in the response spectrum in Figure 4. The small energy in a

1 500 Hz pulse is not sufficient to excite these relatively massive (compared to a one story sub-  
2 urban or rural residence) structures. The impulse is so small (due to its extremely small dura-  
3 tion) that it imparts little change in the momentum of the structure. High attenuation and change  
4 in phase along the structure, creates high damping overall and low response.

### 5 5.1 *Integration of velocity time history*

6 As described in the introduction, strains associated with the fundamental, dominant, or first  
7 mode of response can be calculated from time correlated displacements, which were developed  
8 by integrating the velocity time histories. Before calculation of strains, the velocity time histo-  
9 ries were corrected for baseline irregularities. An example of the four steps in this correction  
10 process is shown in Figure 5. First, the velocity time history (a) is baseline corrected. Linear  
11 and second order polynomial baseline corrections were tested as shown in (b). As can be seen  
12 the polynomial correction did not remove the low frequency (~ 2 Hz artifact) that is not in the  
13 original velocity time history. It was removed by subtracting the 200 point central-moving-  
14 average (continuous line) (c) to produce the displacement time history that oscillates about 0  
15 as shown in (d).

### 16 5.2 *Differential displacement calculation*

17 Prior to the calculation of strains, the differential structure motions were computed from the  
18 difference between displacements at the upper, A, and lower, B, transducer positions as illus-  
19 trated in Figure 6 for event 06/06. Velocity time histories are first integrated using the proce-  
20 dure described in the previous section to obtain displacement time histories. Then the differen-  
21 tial displacement is found by simple subtraction of the two displacements (at A & B) at the  
22 same time. These differential displacements are then searched for the largest. Plots of the trans-  
23 verse velocities recorded at upper and lower transducers of Building 1, as well as corresponding  
24 displacements and differential displacements time histories for the 06/06 event are shown in  
25 Figure 6.

26

27 Table A in the Appendix compares the maximum calculated differential displacements be-  
28 tween measurement points and PPV's induced by all eight events. The maximum recorded  
29 whole or super-structure differential displacement was 334.4 $\mu$ m between the rock (G) and  
30 lower (B-street) levels at the north corner of building 1 during the 06/09 event. The maximum

1 calculated differential displacement between bottom (B) and top (A) was 178.7  $\mu\text{m}$  at the north  
2 corner of the building 1 during the 07/07 event.

3

4 Appendix B contains all velocity and displacement time histories for events 06/06 and 06/09.

## 5 6 STRAIN CALCULATIONS

### 6 6.1 Procedure for calculating strains

7 Two types of strain can be calculated: a) distortion parallel to the plane of the wall and b)  
8 distortion perpendicular to the plane of the wall (Dowding, 2000). First consider distortion  
9 parallel to the plane of a building wall, which produces shear strains that can be calculated as:

$$\gamma = \frac{\delta}{L} \quad (1)$$

10 where L is the wall or building height and  $\delta$  is the distortion or difference of displacement  
11 between the top and bottom of the wall in a direction parallel to the plane of the wall . This  
12 shear strain can be translated into tensile strains,  $\varepsilon_t$ , as follows:

$$\varepsilon_t = \frac{\delta}{L} \sin \varphi \cos \varphi ; \quad (2)$$
$$\varphi = \arctan(H/W)$$

13 where H is the wall height (or in this case the vertical distance between transducer location)  
14 and W is the width (not thickness) of the wall or building face on which the transducers are  
15 located. The H and W's employed in these calculations are visible in Figure 2 and are enumer-  
16 ated in a footnote in the Appendix A table.

17

18 Now consider distortion in a direction perpendicular to the plane of the wall, which produces  
19 bending strains in the wall. A beam deflection model with a measured relative displacement,  
20  $\delta$ , requires a deflection shape to calculate strains. The deflection shape is controlled by the end  
21 conditions of the beam, which can be fixed or free. A “fixed-fixed” end condition describes the  
22 most distorted shape consistent a single maximum  $\delta$ , and was used to calculate the strain from  
23 the relative displacement,  $\delta$  , between two transducers

$$\varepsilon = \frac{6\delta c}{L^2} \quad (3)$$

24 where c is the distance from neutral axis to most extreme fiber, taken here as half the wall  
25 thickness and L is the length of the beam or in this case the height of the wall or distance  
26 between the two transducers, H. For calculations in this study, the walls were assumed to be



1 180 mm (7 in) thick. The fixed-fixed end condition describes the most distorted shape and thus  
2 the highest strain with a single relative displacement,  $\delta$ , that is measured or estimated through  
3 single degree freedom response analysis. The other distortion shape consistent with a single  $\delta$ ,  
4 is “fixed-free”, strains would be one-half that for “fixed-fixed”. Fixed-fixed and fixed-free dis-  
5 tortion shapes are illustrated in mechanics of materials and structural analysis text books and  
6 Dowding (2000).

## 7 8 6.2 *Induced Strains*

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10 Appendix A enumerates and compares all the PPV’s and maximum strains induced in the  
11 two buildings by the eight blast events. As described above these strains were calculated from  
12 the differential displacements that are also compared in this table. Maximum and minimum  
13 global (A-B) in-plane shear strains were 15.0 and 0.3 $\mu$ -strains respectively. Corresponding  
14 maximum in-plane tensile strain calculated was 2.8 $\mu$ -strains.

15  
16 The blast induced strains are low despite high excitation particle velocities. They vary from  
17 blast to blast as would be expected. All of the strains are smaller to the south in building 1,  
18 which is some 60 m south of the blasts located at the north corner as shown in Figure 1. This  
19 consistently smaller differential displacement (A-B) results from the attenuation of the ground  
20 motions along the base of the structure. North to south declination on strain ranges from 75%  
21 to 97% for the radial strains and from 70% to 96% for the transverse strains.

22  
23 Reduction of the number of examples in Appendix A to those in Table 1 with rock excitation  
24 motions more simply illustrates these observations and those to follow. Among other things it  
25 compares basement responses (columns 1-5) with those of the upper stories (columns 6-10).  
26 Basement response is complex. While in-plane shear and tensile strains in the basement can be  
27 calculated from the differential displacements there is no amplification or whole body synchro-  
28 nous response. There is no amplification because superstructure and component natural fre-  
29 quencies fall on the extreme displacement boundary of the response spectrum in Figure 4. The  
30 structures are too massive to respond. In addition the street level floor is not free to move  
31 laterally as is the building above because the basement walls supporting it are restrained from  
32 lateral movement by the soil and infrastructure surrounding the basement walls. This restraint  
33 further reduces the energy transmitted to the floors above as shown in the discussion below.

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Comparison of basement and upper story strains show the degree to which the differential displacements decline in the above-ground section of the building. The ratio between the upper building shear strains (columns 6-10) and the basement shear strains (columns 1-5) ranged from 10% to 73% in the transverse direction. As discussed above this declination is expected as the lower portion of the building absorbs the vibratory energy first. The greatest declinations of strains above the basement level occurred with rock motions at the north end of building 1 that exceeded 75 mm/s (3 ips). The largest excitation motion was some 200 mm/s (8 ips). These high PPVs occurred at dominant frequencies of greater than 250 Hz.

6.3 *Basement Wall response at building 2*

There is one basement location where there can be response without interaction with the surrounding soil and below-ground infrastructure: out of plane bending of the west basement wall adjacent to the excavation. Response of the basement mid-wall (W) transducer in Building 2 to the 08/05 blast demonstrates the extent to which the basement wall responds in this direction. This location is of particular interest as it is the only basement wall that 1) can respond freely without interaction with the surrounding soil and 2) is distorted directly by rock motions. Walls separating above-ground floors are excited by motions transmitted by the building, which decline significantly with distance from the blast location and elevation within the building.

Displacements of the mid wall (W) basement transducer at building 2 are employed to calculate tensile bending strains for shot h, and are compared to the others in Table 1. The out of plane, beam bending model is employed with time correlated displacements measured in the rock (G) and at the street level (B). The L distances needed for this calculation were those shown in Figure 2. As shown in Figure 7, three values of the relative transverse displacements,  $\delta$ , can be calculated: either a) SBT-W, or b) W-GT components, or c) Wall- average (SBT-GT). Differential displacements between the transverse rock (GT) and mid-wall (W) motions are shown in Figure 8 (a) in relation to the velocity and displacement time histories.

The out of plane basement wall response is not large. The PPV of the mid-wall was 7.1 mm/s with a rock excitation of 5. 2 mm/s at 140 Hz. Calculated tensile bending strains of 0.8 to 2  $\mu$ -

1 strains are similar to the tensile strains calculated from the in-plane shear strains in walls above  
2 the street level. They are small compared to the stains that are necessary to cosmetically crack  
3 brick mortar and weak wall covering (300 to 500  $\mu$ -strains) (Siskind2000).

#### 4 *6.4 Comparison with previous studies of tall structure response in urban close-in* 5 *blasting*

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7 Strains measured in this study are lower than those observed in similar tall urban structures  
8 (Aimone-Martin, et al, 2014). Figure 9 compares data from this case with that of others by  
9 comparing calculated tensile strains with peak ground displacement up to 0.1 mm. Aimone-  
10 Martin data are presented as the insert to Figure 9, with both the figure and insert possessing  
11 the same range of shear strains (up to 7  $\mu$ -strains). While this study included situations with  
12 greater peak ground displacement, smaller strains were induced at the higher peak ground dis-  
13 placements and fall below the lower limit curve (A) and upper limit bound (B). The upper  
14 bound of all strains vs peak ground displacement is not exceeded.

#### 15 *6.5 Measured strains are low despite the large magnitude of the peak particle velocity* 16 *in the foundation rock.*

17 The potential for these measured strains to produce hair line, cosmetic cracks can be assessed  
18 by comparison with failure strains as reported by (Aimone-Martin, Meins, 2014) and summa-  
19 rized as follows. Visible surface cracks were observed in the weakest materials found in build-  
20 ings at 300  $\mu$ -strains in drywall plaster core and aged mortar. Onset of visible mortar cracks  
21 between concrete masonry units appeared at 470  $\mu$ -strains (Siskind, 2000). No information is  
22 available in the U.S. literature on nonmilitary dynamic testing providing failure strains for lime  
23 and gypsum plasters typically used as wall coating in historic and older structures. Laboratory  
24 testing of typical Brazilian cement grout samples made with varying cement, lime, and water  
25 ratios and used for surface wall coating is reported by (Rosenhaim, et al (2014). Diametral and  
26 beam bending test results show failure strains range from 153 to 286  $\mu$ -strains. Therefore, a  
27 conservative threshold of 100 to 200  $\mu$ -strains can be employed as an indication of possible  
28 hairline cracking in historic plaster in the above ground portions of the structures.

## 1 7 SINGLE-DEGREE-OF-FREEDOM (SDOF) MODEL

### 2 7.1 *General Considerations*

3

4 Single Degree Of Freedom (SDOF) modeling of structural response is advantageous be-  
5 cause it takes into account the time history of the excitation motion (dominant excitation fre-  
6 quency) as well as amplitude (PPV). Comparative SDOF modeling is instructive in this case  
7 since it returns relative displacement which is directly comparable with measured relative dis-  
8 placement. Since displacements are measured in the plane of the wall comparisons are made  
9 with excitation velocity time histories measured in a direction parallel to the response motions.

10

11 SDOF models consist of a mass, spring and dashpot, for which the relative displacement  
12 response of the spring can be calculated from the excitation motions at the base of the spring.  
13 The dynamic response properties of the structure can be defined by the natural frequency and  
14 percentage of critical damping. This model is described structural dynamics texts as well as in  
15 Dowding (2000). The model returns relative displacement for a given excitation motion, the  
16 maximum of which can be plotted as a pseudo velocity response for a range structural natural  
17 frequencies ( $F_n$ ) and a common damping constant (5% in this case) as shown in Figure 4.  
18 Pseudo velocity is the relative displacement times the circular natural frequency of the struc-  
19 ture, or  $\delta * 2\pi * F_n$ .

20

21 Considerations of energy and mass show that response of large, urban structures to ultra-  
22 high frequency excitation is likely to be low. First consider single degree of freedom (SDOF)  
23 pseudo velocity response with 5% damping of the 06/02 event compared to shown with that  
24 from a large, distant quarry (Q) and close, tunnel (T) blast shown in Figure 4. Spectrum T was  
25 developed from ground motions recorded 12m (38ft) away from a 0 to 9 ms delayed tunnel  
26 blast with a maximum charge in any single delay of 1.7 kg (3.8lb). Spectrum Q was developed  
27 from the ground motions recorded 72m (220ft) away from a single 91 kg (200lb) charge deto-  
28 nated in a typical bench blast hole in a limestone quarry. The quarry blast generated a peak  
29 radial particle velocity of 43 mm/s (1.7 in/s) and the tunnel blast generated a peak radial particle  
30 velocity of 61 mm/s (2.39 in/s) (Dowding, 2000). The 06/02blast generated a radial peak par-  
31 ticle velocity of 51 mm/s in the rock from a 2.4 kg blast some 9+ m distant from building 1.

32

1 Even though the peak particle velocities are similar, standard pseudo-velocity response spec-  
2 trum analysis in Figure 4 predicts that a single story, 10Hz structure or component will sustain  
3 pseudo response velocities that are 50 and 5 times larger for the quarry and tunnel blasts than  
4 for the 06/02 ultra-high frequency event. Since the pseudo velocity is proportional to relative  
5 displacement for structures with the same natural frequency (10 Hz in this discussion), the  
6 06/02 event would be expected to induce far less relative displacement, strain, and cosmetic  
7 cracking than induced in a typical single story residential structure or 10 Hz component.

## 8 *7.2 Use of SDOF as Control Index*

9 It is instructive to compare measured relative displacement (or strain) with indices for con-  
10 trol of the potential for cosmetic cracking to determine their effectiveness. The most often em-  
11 ployed index is peak particle velocity (PPV) ground motion which is measured immediately  
12 adjacent to the structure in the ground. In urban construction PPVs are measured often on the  
13 structure at the street level or in the basement of the structures because of the lack of ground  
14 between excavation and the structure.

15  
16 Single degree of freedom (SDOF) response can also be employed as an index of cosmetic  
17 cracking using ground motion time histories. It is a more robust index than the PPV because it  
18 includes, as described above, the effects of the frequency of excitation relative to the natural or  
19 fundamental frequency of the structure of concern. SDOF systems can be employed for both  
20 single and multiple story structures. Calculations (Dowding, 2000) have shown that the ratio  
21 of pseudo velocity response divided by the excitation peak particle velocity calculated with a  
22 SDOF system is within 15% of the same ratio when calculated with a three floor or three  
23 degree of freedom system (Dowding, 2000). These calculations were made with excitation mo-  
24 tions that were at the 2<sup>nd</sup> and 3<sup>rd</sup> mode frequencies (2.8 and 4.5 times the fundamental fre-  
25 quency). The SDOF response index is employed herein only as an index of the severity of  
26 imposed strains.

27  
28 As shown in Appendix A relative displacements and strains induced in urban structures by  
29 ultra-high blast induced rock motions are very small; 30  $\mu\text{m}$  in the basement and 3  $\mu$  strains in  
30 the super structure for 50 mm/s PPV excitation. Their minimal magnitude is further illustrated  
31 in Table 1 by comparing urban structure responses with those of a variety of residential struc-  
32 tures to surface coal mining blasts (Dowding & McKenna, 2005). Measured (structure-ground)

1 differential displacement (column 3, third column from the left) is compared to the SDOF val-  
2 ues (column 4) calculated from the ground motions. Responses of the 4+ story urban structure  
3 of this study (Building 1) are tabulated in the upper half of the table and those of four single  
4 story residential structures are tabulated on the lower half. Measured displacements are those  
5 from time correlated differences of integrated velocities, and SDOF calculations were made  
6 from the ground or rock excitation motion with 5% damping. SDOF calculations were made  
7 for a range of response frequencies that included both the natural frequency of the superstruc-  
8 ture (10 residential and 2.5 Hz urban) and those of walls and attachments (15 residential and  
9 16 Hz urban).

10  
11 Comparisons in Table 1 allow several observations to be made. As illustrated with the re-  
12 sponse spectra in Figure 4, ultra-high frequency excitation should produce significantly lower  
13 responses than lower frequency excitation with similar PPV's. Table 1 verifies this observation  
14 with the exception of shot d, which will be discussed below. Measured relative displacement  
15 in column 3 of the urban structure with an excitation PPV of 27 mm/s is 20  $\mu\text{m}$  while for a  
16 residential structure with an excitation PPV of only 8 mm/s it is 250  $\mu\text{m}$ . The ratio of (residen-  
17 tial strain to urban strains) per (residential PPV to urban PPV) is some  $(200/20)/(8/27) = >34$ .  
18 Measured relative displacements also match those calculated from SDOF response with ground  
19 motion time histories for both the high (urban) and low (residential) frequency excitation  
20 ground motions.

21  
22 Estimating expected relative displacements for high frequency response of urban structures  
23 on the basis of PPVs yields estimates that are opposite to that measured. If relative displace-  
24 ment is a function of PPV only, and experience with residential structures indicates relative  
25 displacements of 200  $\mu\text{m}$  are produced by PPVs of 6 mm/s then shots b and d should have  
26 produced relative displacements of  $200 \cdot (130 \text{ to } 200)/6 = 5300 \mu\text{m}$ . Measured relative dis-  
27 placements produced by excitation with PPVs of 25 mm/s at ultra-high frequencies are only 20  
28  $\mu\text{m}$ , which is less than  $1/100^{\text{th}}$  of that expected from experience with low frequency excitation  
29 of residential structures, if PPV is employed at the index. Calculated response (based on SDOF  
30 calculation) more closely matches that measured.

31  
32 A comment about shot d and its SDOF calculation is necessary as it is unusual. The measured  
33 relative displacement between the rock and first floor was similar to that calculated with the  
34 SDOF response. As shown by the time histories in Appendix B shot d's high PPV was produced

1 by a single velocity pulse at 500 Hz which was incapable of displacing the first floor by more  
2 than  $1/10^{\text{th}}$  that of the excitation displacement because of its low impulsive energy. Even with  
3 a PPV of some 200 mm/s shot d produced relatively small strains of some 60  $\mu$  strains in the  
4 basement and only 6  $\mu$  strain in the superstructure as shown in Table 1. This absorption of  
5 energy is discussed above and in greater detail elsewhere (Hamdi, 2015)

6  
7 The deminimus magnitude of the measured relative displacements and strains of urban struc-  
8 tures in Table 1 and Appendix A is further verified in Table 1 by crack response data of resi-  
9 dential structures on the right side. The last two columns on the right side of Table 1 compare  
10 response of cosmetic cracks in residential structures to climatological (last column) and blast  
11 vibration (next to last column) (Dowding and McKenna, 2005). Both vibratory and climato-  
12 logical (temperature and humidity) responses are measured by the same micrometer displace-  
13 ment transducer at the same crack location. Comparison of the two right most columns shows  
14 that climatological effects (far right column) produced 5 to 20 times more response of cosmetic  
15 cracks than the blast induced vibratory distortion. This relatively low level of cosmetic crack  
16 response in the residential structures occurred with blast induced relative displacements (dis-  
17 tortions) of 130 to 250  $\mu$  m. (third column from the left). Despite PPV's that exceeded 50 mm/s  
18 the urban structures sustained lower relative displacements and strains (columns 3 and 5) than  
19 did the residential structures with PPV's of 3-8 mm/s, which are in turn 5 to 20 times smaller  
20 than climatological crack response.

## 21 22 8 COMPARISON WITH USBM SAFE BLASITNG CRITERIA FOR RESIDENTIAL 23 STRUCUTRES

24  
25 Impact of ultra-high frequency excitation ground motions can be assessed by comparing  
26 them to the USBM "Z" curve criteria (Siskind, et al, 1980) modified (Aimone-Martin at al,  
27 2014) and European, DIN standards (DIN, 1999). Time histories of the motions of the eight  
28 events were converted to a PPVs- dominant frequency format and plotted with the Z curve in  
29 Figure 10. The second plateau (from the left) in Figure 10 represents a typical 100 mm/s con-  
30 trol limit for blasting adjacent to urban structures with line drilled holes to separate the frag-  
31 mented volume from the rock beneath the adjacent structure. Rock ground motions (solid dots)  
32 are identified by letters defining blasts located in Figure 1 and tabulated in Appendix A. Dom-  
33 inant frequency was determined by calculating the zero crossing times for the pulse with the

1 greatest amplitude. Particle velocities measured at street level (NB & SB) are also plotted as  
2 these are often assumed to be the default motions because of the inaccessibility of the rock  
3 surface.

4  
5 Even though rock motions for shots b,c and d plot above the 100 mm/s control line for fre-  
6 quencies above 200 Hz, the measured relative displacements and strains were small as shown  
7 in Appendix A and Table 1. Generally speaking, the rock motion (circles) displays the highest  
8 frequencies and highest PPVs. Motions at the street level north (triangles) whose frequencies  
9 ranged from 36 Hz to 250Hz fall below the extended “Z” curve control limits.

10  
11 This comparison of excitation motions with and extended “Z” curve control limit demon-  
12 strate the usefulness of additional measurement of structural response. Even though the rock  
13 excitation motions exceeded the 100 mm/s bound above 100 Hz, they induced low relative  
14 displacements and strains in the structure. Thus it has been suggested (Aimone et al, 2014) that  
15 measurement of building response at multiple, structurally significant locations can serve as  
16 the (or a supplemental) mechanism for regulatory control of urban blasting vibrations.

## 17 8 CONCLUSIONS

18 Time correlated velocity response to ultra-high frequency blast vibration excitation was meas-  
19 ured at multiple positions in two urban buildings. These measurements and their analysis allow  
20 the following observations regarding blast induced strains. These observations are based upon  
21 tangential and radial velocity responses at ten positions during eight blast events, which pro-  
22 vided over 70 time histories for analysis. Strains in these multiple story, urban structures are  
23 compared to those measured in one to two story, residential structures, whose response serves  
24 as the basis of many current blasting regulations.

- 25
- 26 • Close-in blasting practice with line-drilling combine to produce ultra-high frequency  
27 excitation pulses with short duration.
  - 28 • Despite high peak particle excitation velocities, differential displacements (and thus  
29 strains) along a structure are similar to and often less than those measured in residential  
30 structures excited by lower than regulation limited peak particle velocities.



- 1 • Strains measured on these urban structures produced by ultra-high frequency, high peak  
2 particle velocities are lower than those necessary to crack masonry structures and weak  
3 wall covering materials.
- 4 • Measurement techniques presented herein demonstrate how strain calculated from dif-  
5 ferential displacement can be employed to control blasting activities.
- 6 • Relative displacement response calculated with damped single degree of freedom mod-  
7 els of the structures generally matches that measured when excitation motions are those  
8 measured in the rock for basement response and at the street level for superstructure  
9 response.

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25

26

27

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# Appendix A

Table A. Strain level estimation in the different parts of the two investigated buildings.

Building	Set	Blast	Shot	Transd	PPV (mm/s)	frq (Hz)	PPV/frq (~mm)	Position	Diff (µm)	S Strain (µ-strains)	T Strain (µ-strains)
1	Set 1	06/30	e	NBR	10.3	111	0.093	NR(A-B)	54.8	4.7	0.9
				NBT	10.8	91	0.119	NT(A-B)	37.4	1.3	1.3
				NAR	6.6	91					
				NAT	6.1	36					
				SBR	2.5	200	0.013	SR(A-B)	7.9	0.3	0.1
				SBT	1.5	111	0.014	ST(A-B)	7.9	0.3	0.1
				SAR	1.5	34					
				SAT	0.9	16					
		06/27	f	NBR	24.4	125	0.195	NR(A-B)	132.8	11.0	2.1
				NBT	17.3	63	0.275	NT(A-B)	136.5	12.0	4.8
				NAR	16.8	63					
				NAT	19.8	63					
				SBR	5.2	59	0.088	SR(A-B)	14.6	0.5	0.2
				SBT	2.9	100	0.029	ST(A-B)	14.7	0.5	0.3
				SAR	2.5	34					
				SAT	1.7	17					
		07/07	g	NBR	19.3	167	0.116	NR(A-B)	178.7	15.0	2.8
				NBT	22.9	77	0.297	NT(A-B)	113.9	9.8	4.0
				NAR	21.3	77					
				NAT	8.5	67					
				SBR	2.4	125	0.019	SR(A-B)	12.1	0.4	0.2
				SBT	1.7	36	0.047	ST(A-B)	10.5	0.4	0.2
				SAR	2	36					
				SAT	1.1	18					
	08/05	h	NBR	7.6	125	0.061	NR(A-B)	17.8	1.5	0.3	
			NBT	6.6	77	0.086	NT(A-B)	21.6	1.9	0.8	
			NAR	3.6	59						
			NAT	4.1	63						
			SBR	4.7	111	0.042	SR(A-B)	8.1	0.3	0.1	
			SBT	1.1	100	0.011	ST(A-B)	12.1	0.4	0.2	
			SAR	1	42						
			SAT	1.1	15						
	Set 2	06/05	b	NBR	12.8	77	0.166	NR(A-B)	62.3	5.4	1.0
				NBT	13.6	125	0.109	NT(A-B)	54.4	4.7	1.9
				NAR	6.1	71					
				NAT	8	29					
				GR	39.4	333	0.118	GR(B-G)	33.1	5.7	2.8
				GT	128.8	500	0.258	GT(B-G)	89.1	15.3	6.3
		06/09	d	NBR	15.7	77	0.204	NR(A-B)	49.7	4.3	0.8
				NBT	9.8	167	0.059	NT(A-B)	69.8	6.0	2.5
				NAR	7.1	71					
				NAT	10.3	59					
				GR	201.4	500	0.403	GR(B-G)	208.7	36.0	0.6
				GT	200.4	500	0.401	GT(B-G)	334.4	57.7	1.3
	Set 3	06/02	a	NBR	6.6	100	0.066	NR(A-B)	32.9	2.8	0.5
				NBT	5.1	59	0.086	NT(A-B)	27.9	2.4	1.0
				NAR	7.1	100					
				NAT	4.4	53					
SBR				9.1	200	0.046	SR(A-B)	19.6	0.7	0.3	
SBT				3.8	200	0.019	ST(A-B)	12.6	0.7	0.4	
06/06		c	SAR	1.5	42						
			SAT	1.7	17						
			GR	51.6	500	0.103	GR(B-G)	33.8	5.8	0.1	
			GT	27.4	333	0.082	GT(B-G)	19.3	3.3	0.2	
			NBR	12.1	83	0.146	NR(A-B)	63.1	5.4	1.0	
			NBT	10.8	143	0.076	NT(A-B)	58.0	5.0	2.1	
Set 2	06/06	c	NAR	6.6	45						
			NAT	10.2	71						
			SBR	4.1	250	0.016	SR(A-B)	11.2	0.4	0.2	
			SBT	2.4	100	0.024	ST(A-B)	15.1	0.6	0.3	
			SAR	2	31						
			SAT	1	15						
	06/06	c	GR	131.6	500	0.263	GR(B-G)	127.1	21.9	0.2	
			GT	70.4	250	0.282	GT(B-G)	72.9	12.5	0.8	
			SBR	3	83	0.036	SR(A-B)	17.8	1.1	0.5	
			SBT	4.1	100	0.041	ST(A-B)	18.7	1.2	0.5	
			SAR	4.1	100	0.041	WT(B-W)	19.1		2.0*	
			SAT	4.1	83						
Set 2	06/06	c	GT	5.2	143	0.036	GT(B-G)	17.4	3.0	1.4	
			GR	19.4	500	0.039	GR(B-G)	17.4	3.0	0.6	
			SAT	2	71						
			GR	19.4	500						
			GT	5.2	143	0.036	WT(G-W)	18.4		0.8*	
			GT	5.2	143	0.036	WT(W-Avg(SBT,GT))	17.5		1.9*	
	08/05	h	W	7.1	50						

\* Bending strains

Distances used for the strain computation:

- H=11.6m and W=22.2m for the North transverse components and H=11.6m and W=61m for the north radial components for the Building 1;
- H=27.4m and W=22.2m for the South transverse components and H=27.4 and W=61m for the south radial components for the Building 1.
- H=5.8m and W=22.2m for the North rock to bottom transverse components and H=5.8m and W=61m for the north rock to bottom radial components for the Building 1.
- H=15.8m and W=7.6m for the transverse components and H=15.8m and W=26.2m for the radial components for the Building 2;
- H=3.5m and W=7.6m for the rock to mid-wall transverse components and H=3.5m and W=26.2m for the rock to mid-wall radial components for the Building 2;
- H=2.2m and W=7.6m for the mid-wall to bottom transverse components and H=2.2m and W=26.2m for the mid-wall to bottom radial components for the Building 2.

# Appendix B

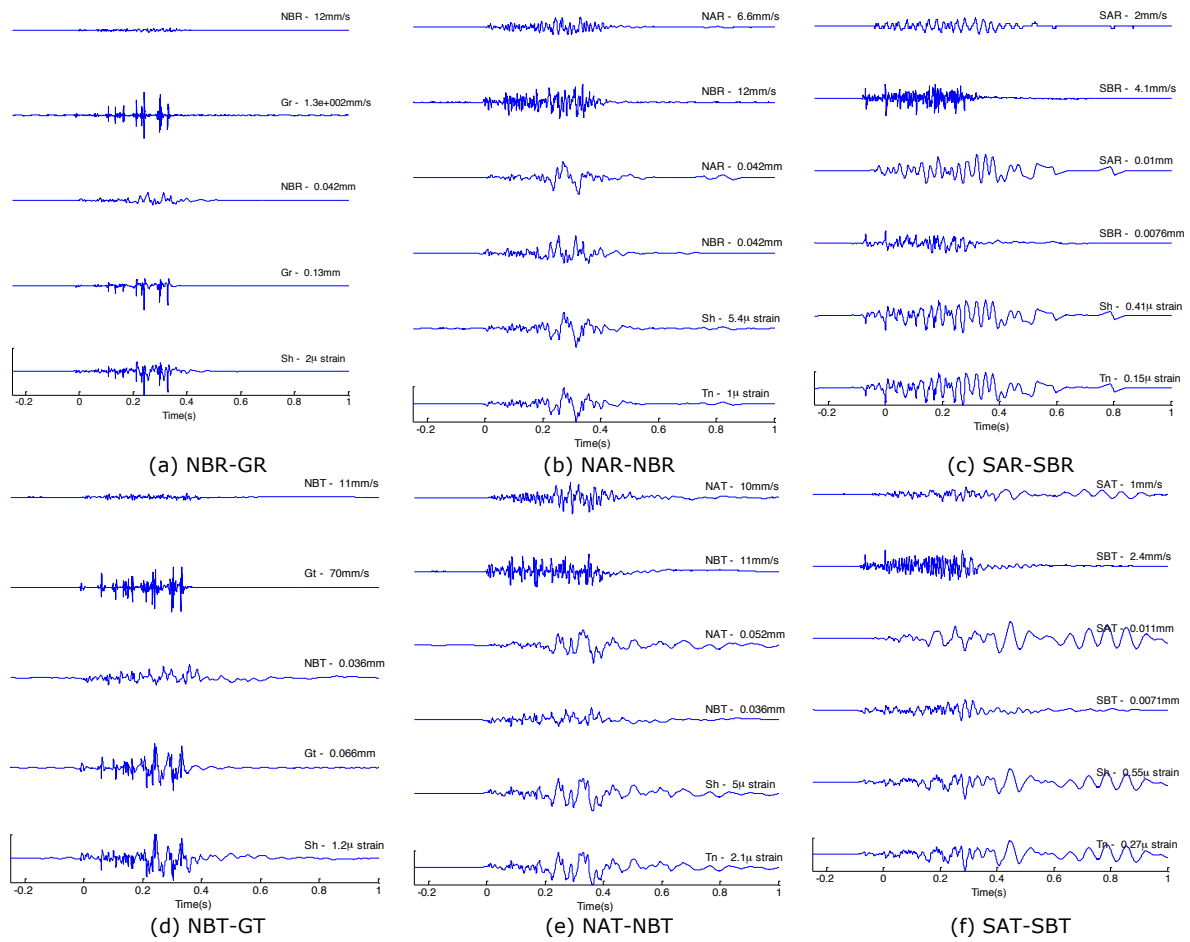


Figure B.1. Strain level calculations for blast 06/06.

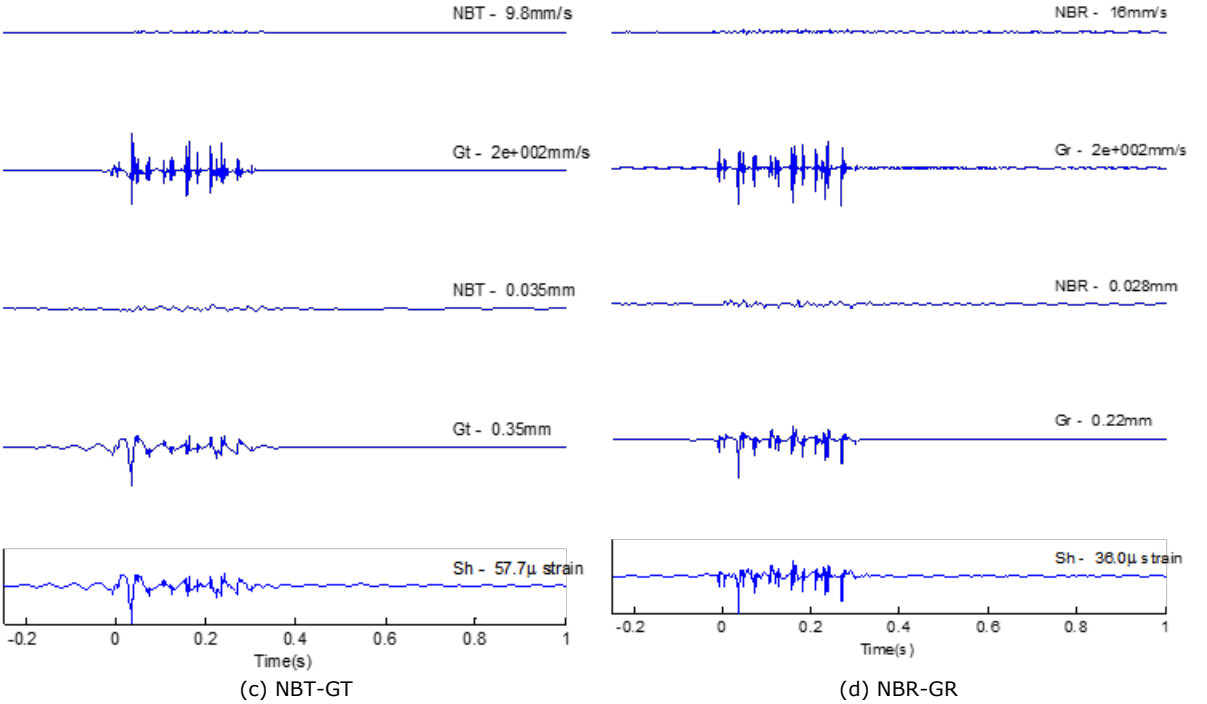
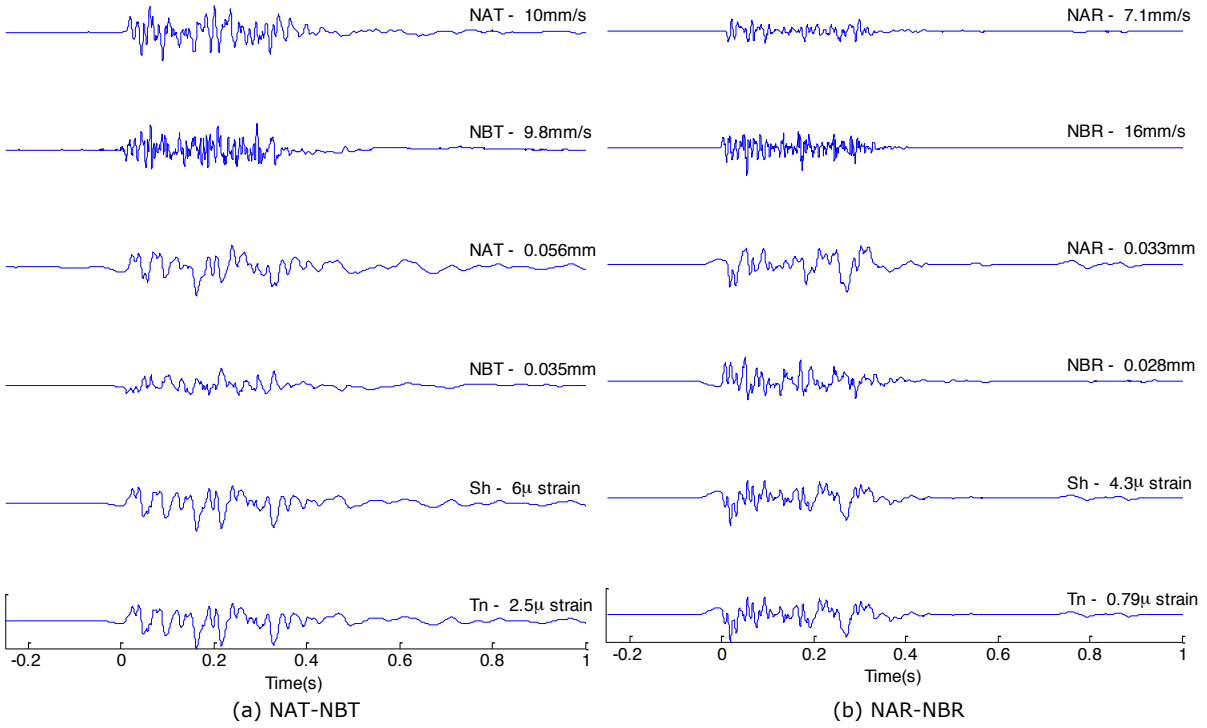
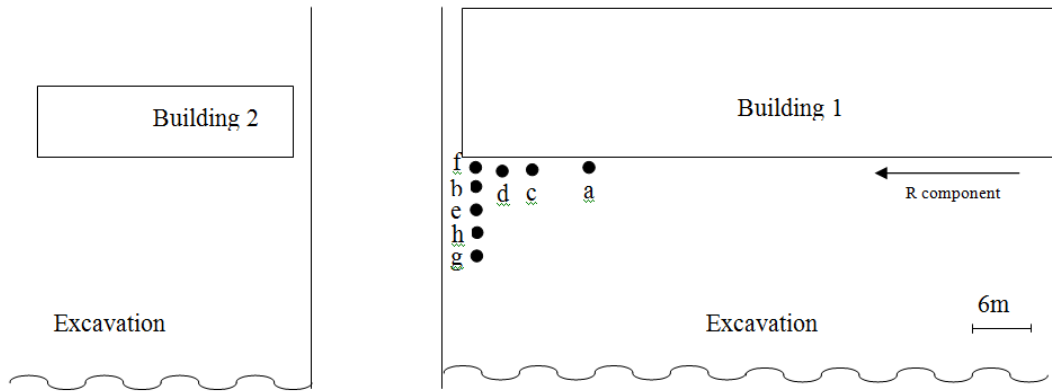
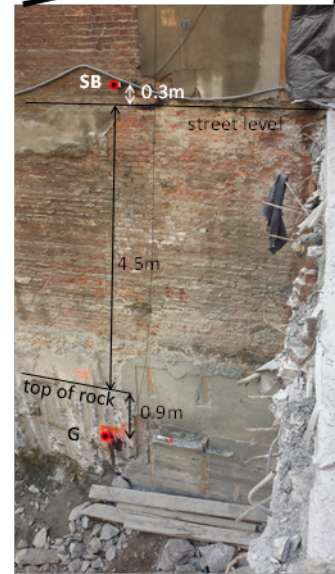
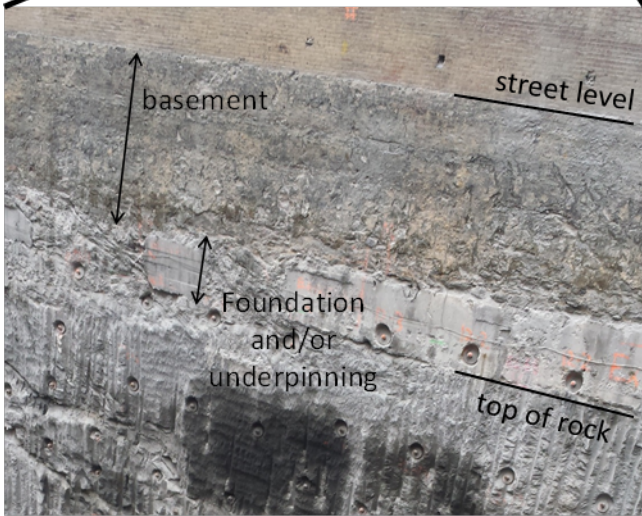
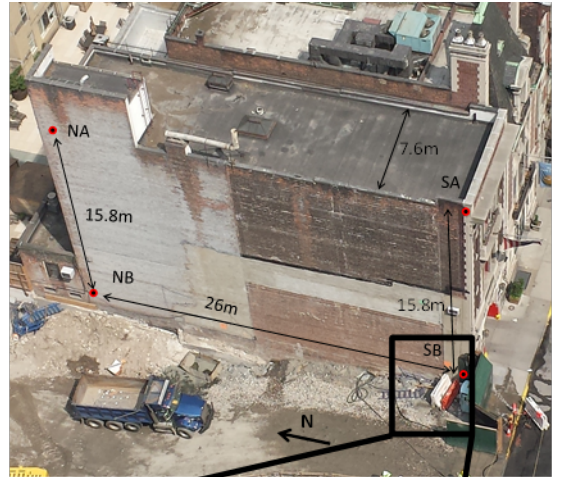


Figure B.2. Strain level calculations for blast 06/09.



*Figure 1. Blast locations with regards to the buildings. The close proximity and simultaneous construction allows blast response from ground motions with high amplitudes and ultra-high frequency to be measured at both buildings. (a: blast 06/02/2014; b: blast 06/05/2014; c: blast 06/06/2014; d: blast 06/09/2014; e: blast 06/27/2014; f: blast 06/30/2014; g: blast 07/07/2014; h: blast 08/05/2014).*



*Foundation details of Building 1*

*Foundation details of south end of Building 2*

*Figure 2. Locations of the sensors at the upper and lower parts of the monitored walls at the two buildings.*

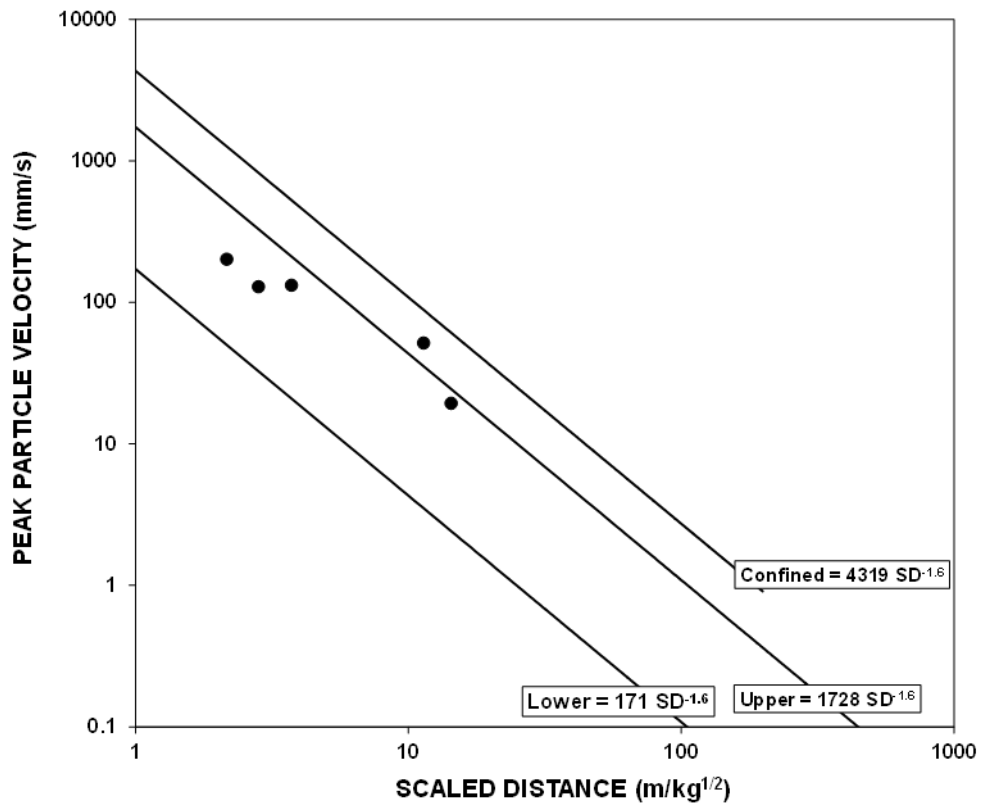


Figure 3. Comparison of measured square root scaled distance attenuation and Oriard's (1972) expected values for typical practice showing the difference between rock to rock transmission (rock data) and rock to street (NB data). Curve C is for confined conditions and B and A are upper and lower bound of expected values.



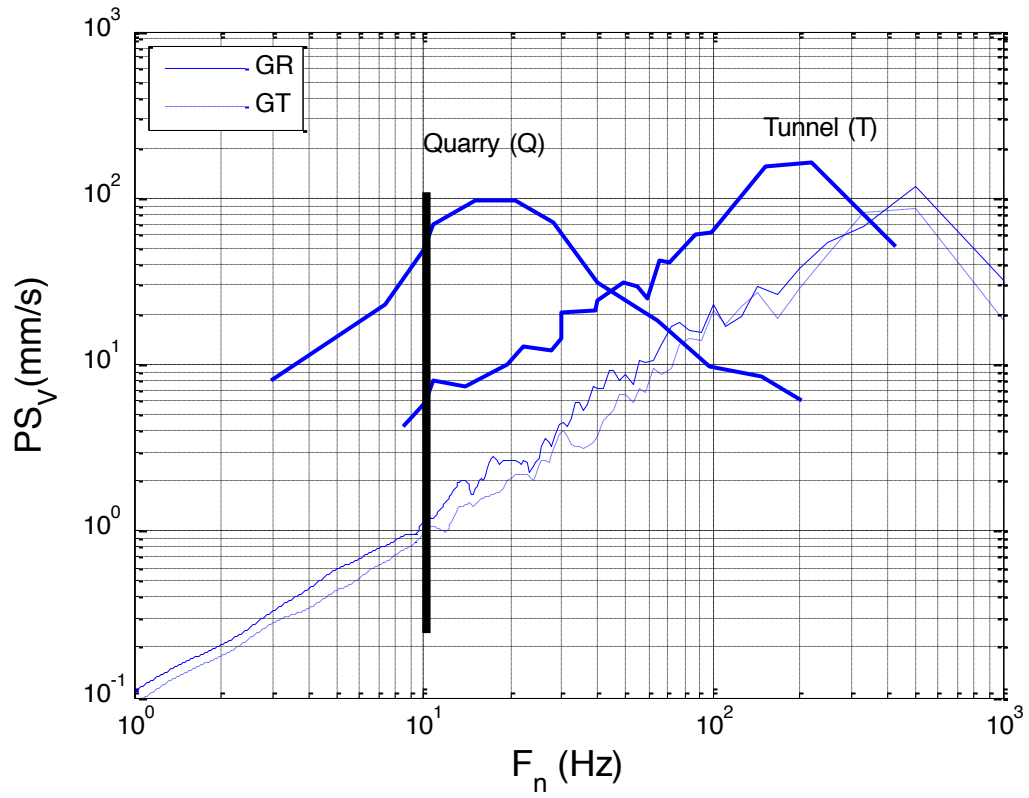


Figure 4. Comparison of response spectra of ground motions from close-in blast event 06/02 and a low frequency quarry blast (Q) and a near-by tunnel blast (T); GR (solid line and generally larger) and GT are rock motions in N-S and E-W directions respectively.

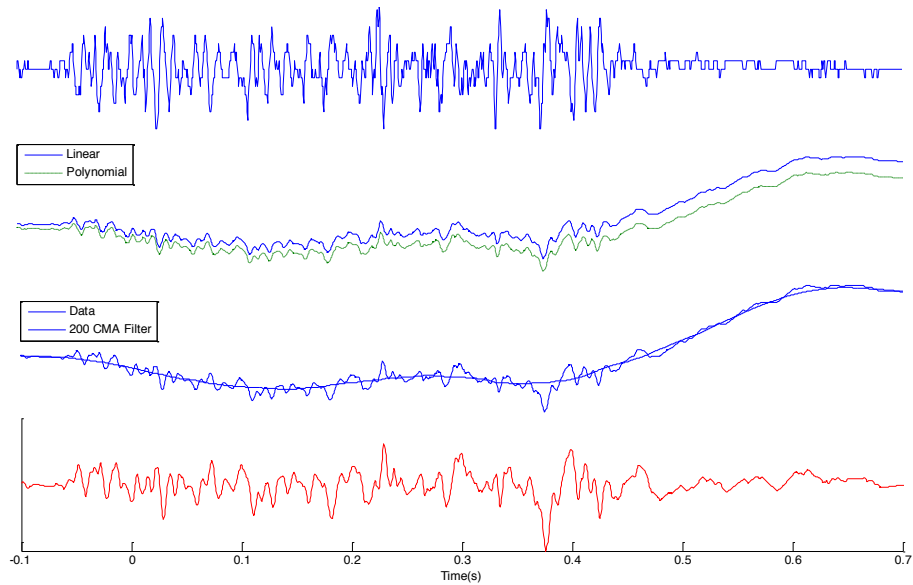


Figure 5. Displacements calculation using baseline correction and 200 point central-moving-average filtering (case of SBT recording at Building 2): (a) (top) Velocity recording, (b) Displacement after linear (solid and generally higher) and second order polynomial baseline correction, (c) 200 point central-moving-average fit to the second order baseline corrected displacement data, (d) (bottom) Final displacement obtained by subtracting the 200 CMA from the data.

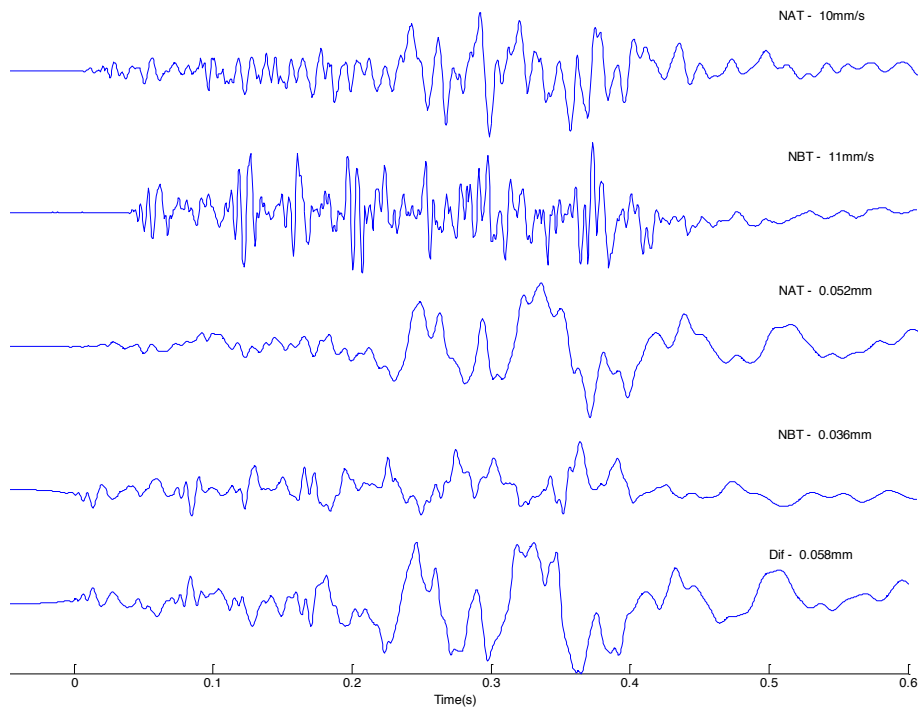


Figure 6. Example calculation of the difference in transverse displacements between the top and bottom of the north corner of building 1 for the 06/06 event: a) top two time histories—velocities at top (NAT) and bottom (NBT); b) middle two time histories – displacements at top and bottom and c) bottom time history – difference between top and bottom displacements. Velocities and displacements are plotted at consistent scales, where the amplitudes given at the right are those of the peaks.

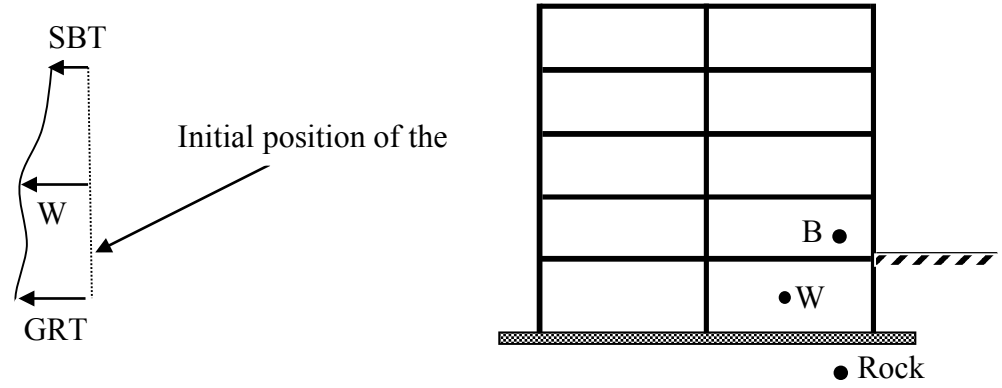


Figure 7. Displacement in the bottom southern part of the wall in Building 2 (W: Mid-wall, SBT: south lower, GRT: transverse ground motion).

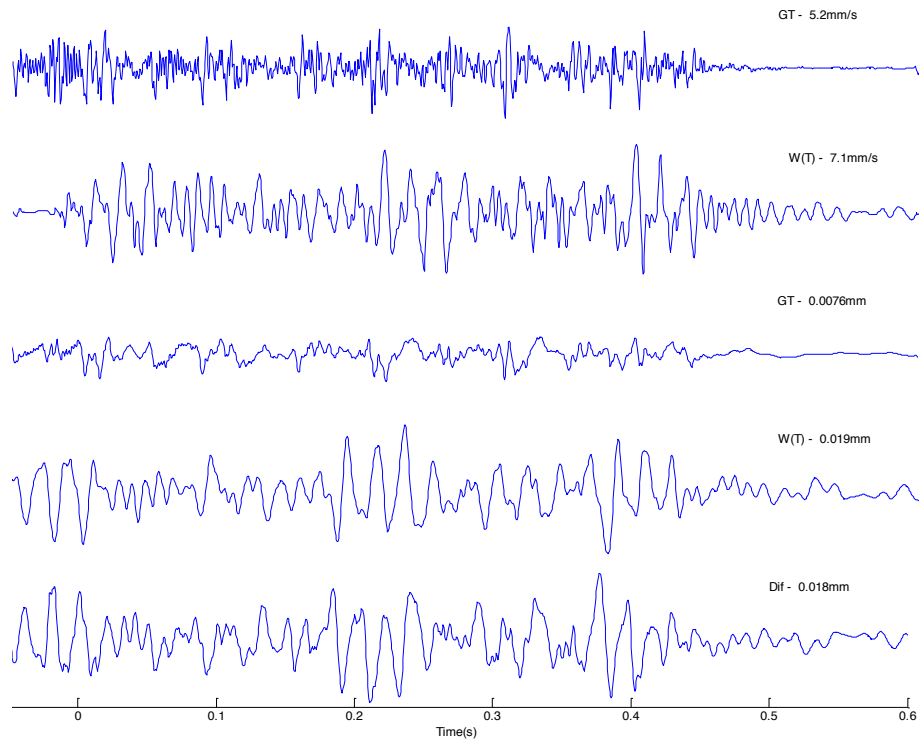


Figure 8. Differential displacements calculation using baseline correction and 200 point central-moving-average filtering (case of rock and mid-wall recordings at Building 2 during blast 08/05/2014): (a) and (b) Velocity recordings, (c) and (d) Displacements after second order polynomial baseline correction, (e) Final differential displacement. Velocities and displacements are plotted at consistent scales, where the amplitudes given at the right are those of the peaks.

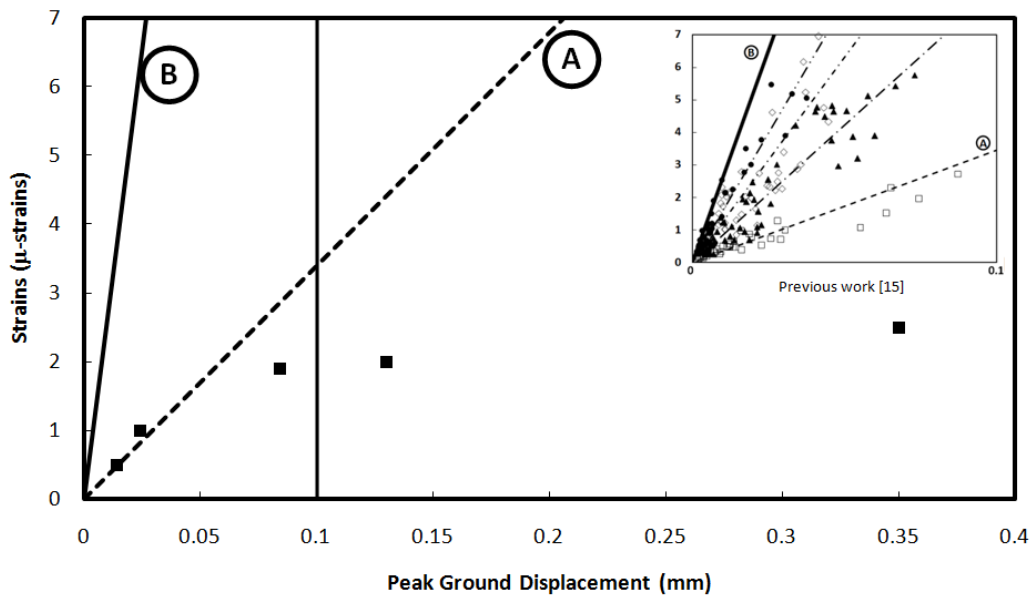


Figure 9. In plane tensile strains at the top and bottom of buildings versus peak ground displacement. Comparison with Aimone et al (2014)

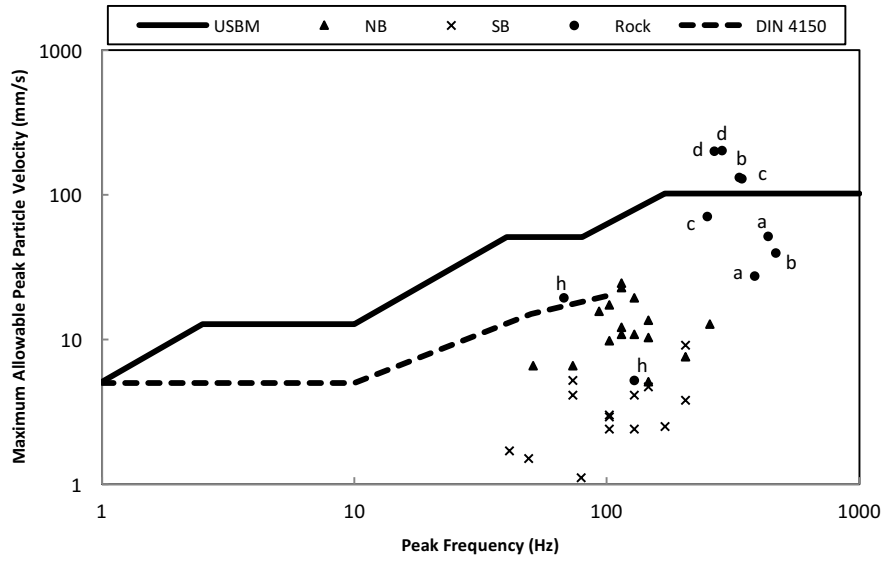


Figure 10. Frequency and Maximum Peak Velocity compared to the safety USBM and DIN 4150 criteria. Extension of the USBM control above 100Hz has been suggested to use with close-in blasting (Aimone et al 2014).

Table 1 Measured and SDOF Calculated Responses of Structures to Low and Ultra-High Frequency Blast Excitation												
	Basement and One Story Response					Above Ground Response					Crack Response	
	PPV Rock	Freq Excite	Relative Displacement Measured	Relative Displacement Calculated Rock	Shear Strain Measured	PPV Grd Floor	Freq Excite	Relative Displacement Measured	Relative Displacement Calculated Street	Shear Strain Measured	Peak Vibration	Max Weather
	mm/s	HZ	µm	µm	µ strain	mm/s	HZ	µm	µm	µ strain	µm	µm
<b>4 to 5 Story Urban Building (1)</b>				2.5-16 Hz	h = 5.8m				2.5-16 Hz	h = 11.6 m		
Shot a	27.4	333	20	14-16	3.3	5.1	59	28	22-27	2.4		
Shot c	70.4	250	72	59-121	12.5	10.8	143	58	31-51	5		
Shot b	132.6	500	89	74-87	15.1	13.6	125	54	36-48	4.7		
Shot d	198.1	500	334	360-471	57.5	9.8	167	70	32-92	6		
<b>4 to 5 Story Urban Building (2)</b>												
Shot h (basement midwall response)	5.1	143	18		2 <sup>1</sup>							
<b>Single Story Residential Structures</b>				10-15 Hz	h = 2.5m							
Trailer: Pennsylvania	3.6	7 to 20	210	240-180	86.1						4.2	24
Bungalow 1: Indiana	5.8	6 to 25	180	170-95	73.8						0.3	12
Wood Frame: Indiana	7.6	15 to 20	133	150-259	54.5						13.6	52
Adobe: New Mexico	8.1	4 to 14	250	230-80	102						0.9	25

1 Bending strain